

Clinical Trial Design for Rare Diseases using Bayesian Bandit Models



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Introduction & Motivation

- ▶ Consider a two-arm clinical trial with binary end points and a finite number of patients, n .
- ▶ Suppose each treatment, A and B , has an unknown success probability, θ_A and θ_B , respectively, and each patient's response is immediately available.
- ▶ The null and alternative hypotheses are formulated as

$$H_0 : \theta_A = \theta_B \text{ versus } H_1 : \theta_A \neq \theta_B,$$

and we assume $\theta_A, \theta_B \sim \text{Beta}(1, 1)$ a priori.

Objective: To design a clinical trial which identifies the superior treatment (explores) whilst effectively treating the trial participants (exploits). This will be particularly useful in trials for rare diseases.

- ▶ This is a natural application area for **bandit models** which seek to balance the **exploration versus exploitation trade-off** to obtain an optimal allocation policy.
- ▶ Bandit models are a type of **response-adaptive design**.
- ▶ Learning takes place during the trial (rather than just at the end as in the traditional randomised controlled trial).
- ▶ The optimality property, in terms of **maximising the expected number of patient successes**, is the primary motivation behind implementing bandit-based designs in clinical practice.

Optimal Design using Dynamic Programming (DP)

- ▶ We use DP to obtain the optimal adaptive treatment allocation sequence.
- ▶ The idea behind DP is a recurrence equation (the Bellman equation), which relates the expected total reward at a given decision time to the distribution of its possible values at the next decision time.
- ▶ We implement a backward induction algorithm in which we start with patient n and proceed iteratively towards the first patient.

Limitations for Trial Design

- ▶ This design is completely **deterministic**.
- ▶ Optimal designs which achieve the highest patient benefit suffer from the **lowest power**.

We focus on modifications to the optimal design which aim at overcoming these limitations without having a significant impact on the patient benefit criterion.

Randomised Dynamic Programming Design (RDP)

- ▶ A natural first step is to modify the optimal DP design by **forcing actions to be randomised**.
- ▶ This helps to **maintain blinding** and **reduce the risk of bias**.
- ▶ We define the following actions so that each treatment has a probability of at least $1 - \rho$ of being allocated to each patient, where $0.5 \leq \rho \leq 1$.

- Action 1:** A patient receives treatment A with probability ρ (and treatment B with probability $1 - \rho$).
- Action 2:** A patient receives treatment B with probability ρ (and treatment A with probability $1 - \rho$).

- ▶ We tried a range of values for ρ and suggest setting $\rho = 0.90$.
- ▶ This design markedly improves power and trades a small reduction in optimality for randomisation.

Further Limitations

- ▶ There is a possibility that all patients may be allocated to only one treatment.

Constrained RDP Design (CRDP)

- ▶ We propose a constrained variant of the RDP design which **ensures that we always obtain at least Y observations from each treatment arm**.
- ▶ Therefore, we can no longer end up with no observations on a treatment arm.
- ▶ To do this, we assign a large negative penalty to every terminal state that has less than Y observations on a treatment arm.
- ▶ This causes the undesirable states to now be avoided.
- ▶ We tried several values for the lower bound Y and suggest setting $Y = 0.15n$.

Simulation Study

We evaluate the CRDP design in several scenarios by simulating 10,000 replications and focusing on the following performance measures:

- ▶ Power; type I error rate; average bias of the treatment effect estimator; mean squared error (MSE) and the percentage of patients allocated to the superior treatment (% on sup).

...and we compare our proposed CRDP design to the following designs:

- ▶ Traditional fixed randomisation; randomised play-the-winner (RPW); Whittle index policy (WI), DP and RDP.

These figures correspond to $n = 75$, $\theta_A = 0.5$ and $\theta_B \in (0.1, 0.9)$.

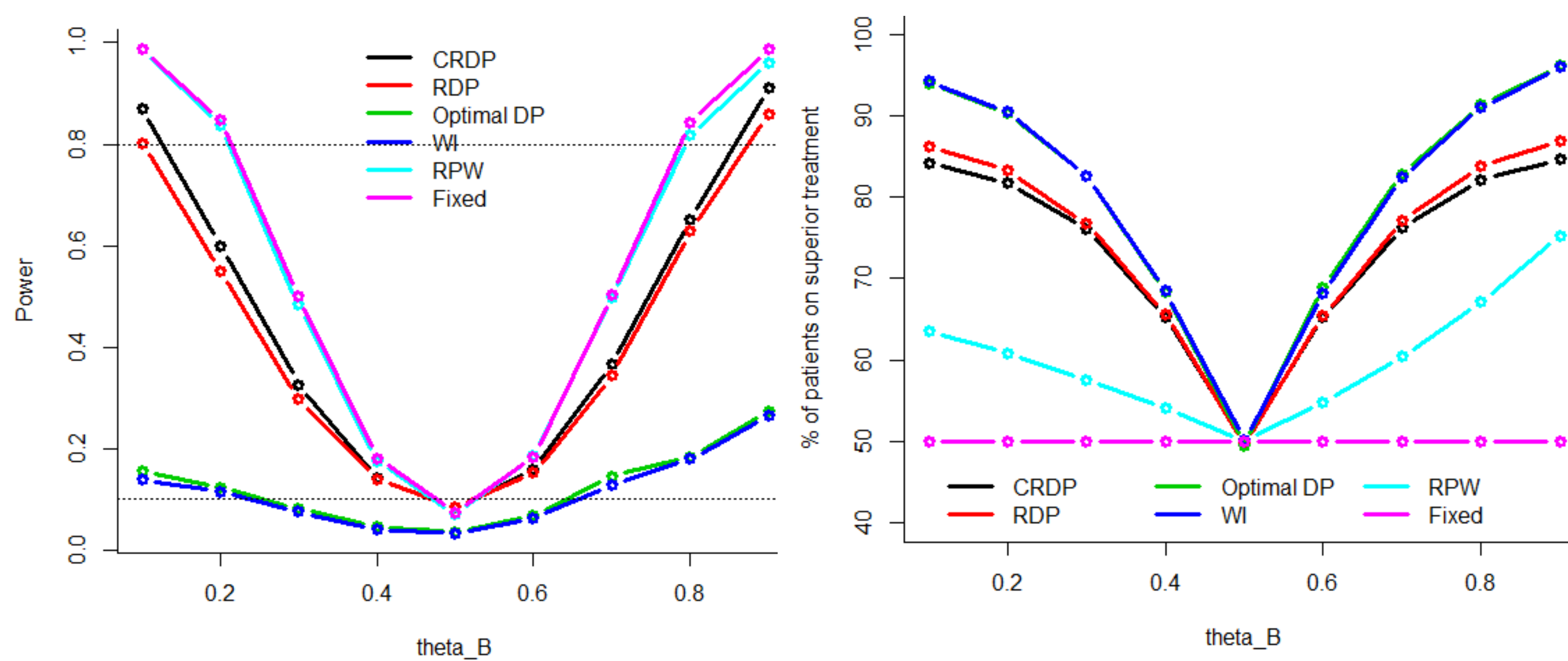


Figure 1: Power and type I error

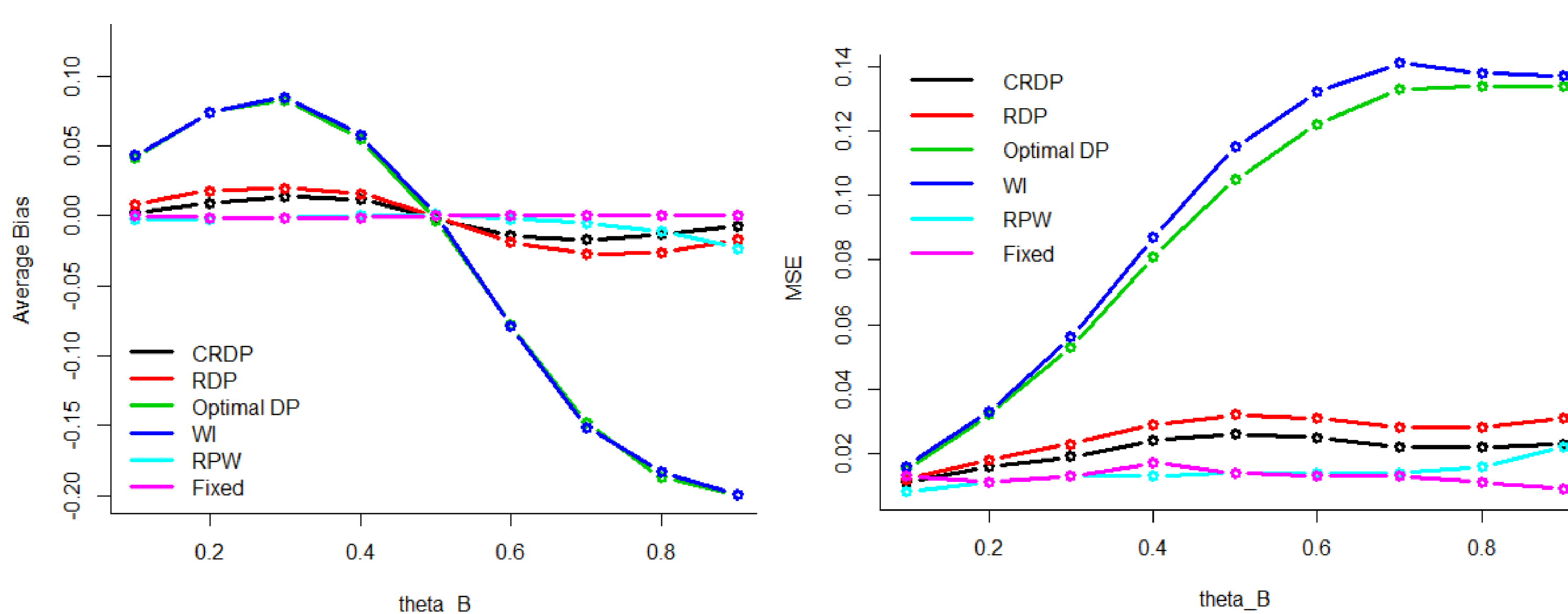


Figure 2: % on sup

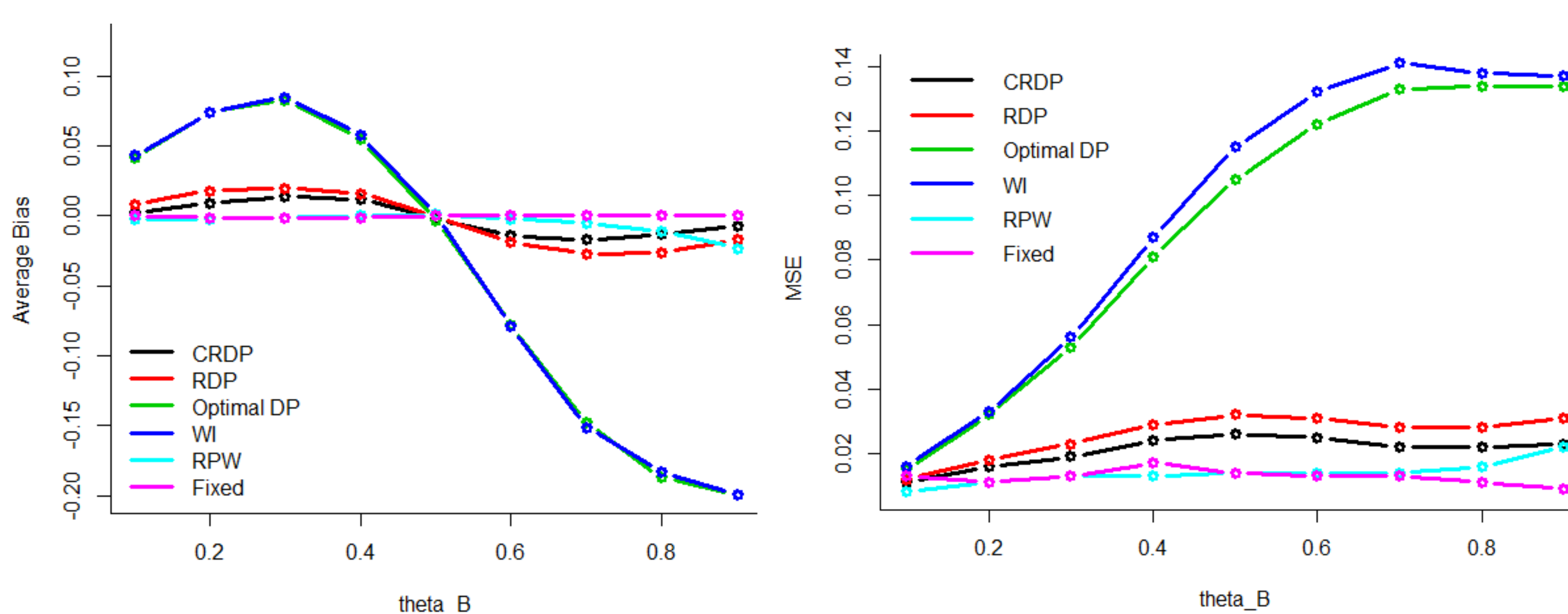


Figure 3: Average bias

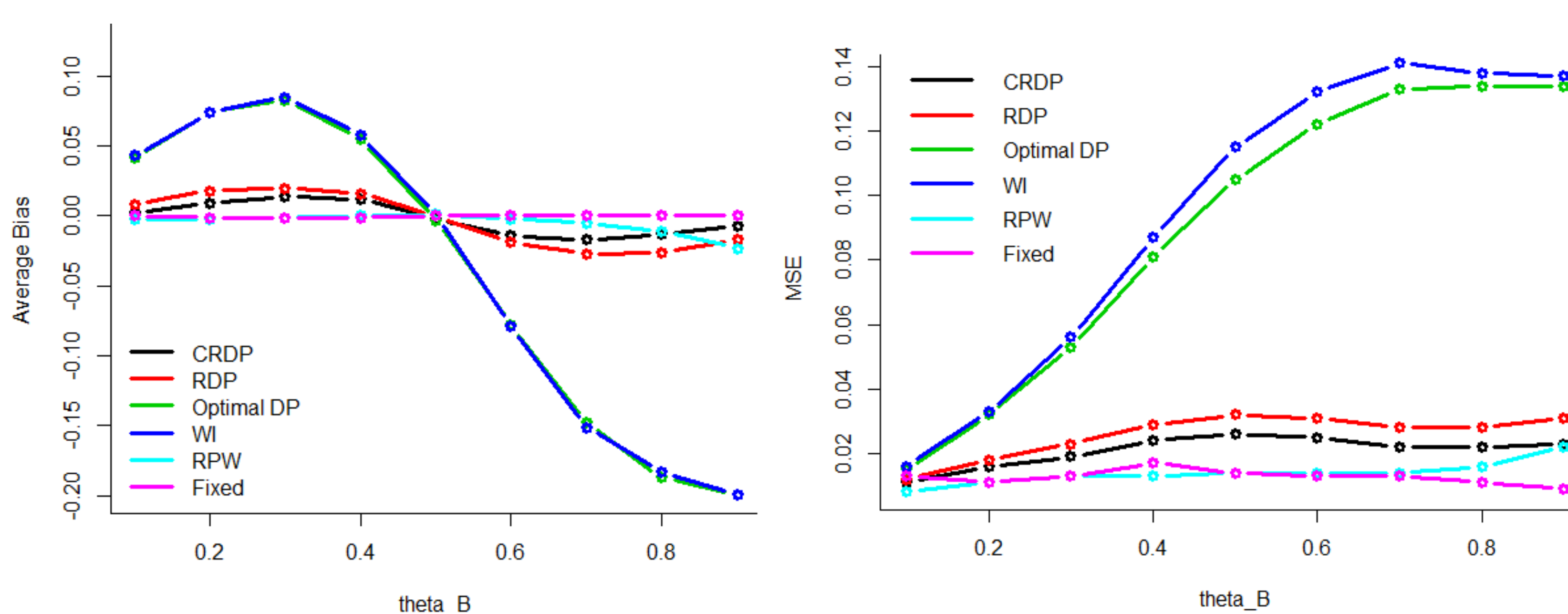


Figure 4: MSE

Conclusions

Our proposed CRDP design produces very promising results:

1. The **power is greatly improved upon** relative to the other bandit designs (Figure 1).
2. The **% of patients allocated to the superior treatment is much higher** than in the traditional fixed and RPW designs (Figure 2).
3. The **bias and MSE of the treatment effect estimator is greatly reduced** compared to the other bandit designs (Figures 3 and 4).

Such designs will be particularly useful for rare diseases in which a substantial proportion of patients exhibiting the disease are included in the trial, and therefore the priority is to treat these patients as effectively as possible.